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## introduction [geting started]

Shooter's Reference V3 is a ballistics calculator for sports shooting enthusiasts that features a classical physics-based projectile motion model, cartridge database, and several other useful tools.

The V3 ballistics model supports G1 and G7 drag models (as well as many others), BC (ballistic coefficient) and ambient weather conditions compensation yielding accurate bullet drop and wind drift solutions. For ease of use, Shooter's Reference has a built-in database of over 2,000 cartridges from Barnes ${ }^{\circledR}$, Buffalo Bore ${ }^{\circledR}$, CCI ${ }^{\circledR}$, Eley ${ }^{\circledR}$, Federal Premium ${ }^{\circledR}$, Fiocchi ${ }^{\circledR}$, Hornady ${ }^{\circledR}$, Norma-USA ${ }^{\circledR}$, Nosler ${ }^{\circledR}$, $\mathrm{PMC}^{\circledR}$, Remington ${ }^{\circledR}$, Weatherby ${ }^{\circledR}$, and Winchester ${ }^{\circledR}$. In addition, the user can manually enter the required input parameters such as muzzle velocity and bullet weight.

Additional tools are included that aid sight-in calculations at the range, estimating the distance to a target, and performing mils and moa calculations.

Both imperial and metric units are supported.
Comments, complaints, suggestions, and questions are appreciated.


Contact Us support@ttfsapps.com

## WARNING! <br> PRACTICE SAFE FIREARMS HANDLING AND FOLLOW ALL SAFETY RULES! ALWAYS!!!

## search [find your cartridge's specs in the built-in database]

## Cartridge Database

In order to set up the ballistics calculator, there are a few parameters you need to know about your cartridge. We have included a database of over 2,600 popular rifle and handgun cartridges that can be searched simply by tapping the search boxes on the search page. Tap the products box to see the list of cartridges that match your criteria and to choose one. Note that a maximum of 100 products can be displayed. The best way to avoid that limit is to choose a cartridge.

The parameters required by the ballistics calculator are automatically loaded into the setup page when a product is selected. The following parameters are extracted:

- Bullet diameter
- Bullet weight
$\oplus$ Ballistic coefficient (optional, not required)
- Muzzle velocity
- Muzzle energy (not used, but displayed)
SHOOTER'S REFERENCE V3
search specs s
firearm type
Center Fire Rifle
cartridge
338 Lapua Magnum
ammo use
tap to select
manufacturer
Winchester
products
Winchester GM338LM
$\square$Use lookup page to automaticallyenter ballistics data, if available.

Use lookup page to automatically enter ballistics data, if available.

## CROWN MOLDING

Any angle. Any place. Calculate once and measure twice!

And it's FREE!

## SPeCS [view manufacture's data and description]

## Cartridge Specs

When a cartridge is selected from the database, a summary of the its specifications is displayed on the specs page. The specs are from the manufacturer and are subject to change.

Typically, the following specifications are available:

- Manufacturer, product line, and part number
- Cartridge and bullet description
- Typical application
- Bullet weight and ballistic coefficient
- Muzzle velocity
† Muzzle energy


## SHOOTER'S REFERENCE V3 <br> specs setup so

manufacturer's specs
Manufacturer: Winchester
Firearm Type: Center Fire Rifle
Part Number: GM338LM
Cartridge: 338 Lapua Magnum
Cartridge (metric): $8.6 \times 70 \mathrm{~mm}$
Bullet: BTHP
Product Line: Sierra® MatchKing ${ }^{\circledR}$
Application: Competition
Bullet Weight (gr): 250
BC: 0.587
Velocity Muzzle: 2950
Energy Muzzle: 4830

i)
Use lookup page to automatically enter ballistics data, if available.

CROWN MOLDING
Any angle. Any place. Calculate once and measure twice!

And it's FREE!

## SEtUP [setup model parameters]

## Model Setup

## Cartridge and Bullet Parameters

These parameters describe the cartridge and bullet.

## © bullet caliber

- Required, inches or mm, depending common usage
$\oplus$ bullet weight
- Required, always in grains
$\dagger$ ballistic coefficient
- Only required if use bc box is checked
- Default is to not use BC in ballistics model (yields best results)
- Can be applied to any of the bullet models but most manufacturers only specify a G1 BC
- bullet model
- Required, G7 default
- G7 works best for low drag bullets
- See page 30, Standard Bullet Models for more information

SHOOTER'S REFERENCE V3

## setup solve ho

| cartridge an bullet caliber [in or mm ] | bullet para bullet weight [gr] | bullet bc | bullet model |
| :---: | :---: | :---: | :---: |
| 0.338 | 250 | 0.587 |  |
| muzzle velocity [fps] | muzzle energy [ft-lbs] | use bc | G5 |
| 2950 | 4830 |  |  |

ambient conditions

| wind speed <br> [mph] | wind direction <br> [deg] | elevation <br> [ft] |
| :---: | :---: | :---: |
| 15 | 270 | 0 |
| temperature <br> [deg F] | humidy <br> [rh \%] | pressure <br> [in Hg ] |
| 59.0 | 78 | 29.53 |

firearm setup
scope height zero dist
[in] [yds]
1.5

200

scope height zero dist


## SEtUP [setup model parameters]

## Model Setup (continued)

## Cartridge and Bullet Parameters (continued)

$\oplus$ use bc

- Not required or recommended
- If checked, ballistics model applies BC to selected bullet model's drag coefficient
- muzzle velocity
- Required, in fps or mps
- muzzle energy
- Displayed for information only, in ft-lbs or Joules

SHOOTER'S REFERENCE V3

## setup solve ho

| cartridge an bullet caliber [in or mm] | bullet paran bullet weight [gr] | bullet bc | $\begin{aligned} & \text { bullet } \\ & \text { model } \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| 0.338 | 250 | 0.587 |  |
| muzzle velocity [fps] | muzzle energy [ft-lbs] | use b | G5 |
| 2950 | 4830 |  |  |

ambient conditions

| wind speed [mph] | wind direction [deg] | elevation [ft] |
| :---: | :---: | :---: |
| 15 | 270 | 0 |
| temperature [deg F] | humidy <br> [rh \%] | pressure <br> [in Hg ] |
| 59.0 | 78 | 29.53 |
| firear scope height [in] | setup zero dist [yds] | units |
| 1.5 | 200 | metric |

firearm setup
scope height zero dist
[in] [yds]
1.5

200
units check for
metric

## SEtUP [setup model parameters]

## Model Setup (continued)

## Ambient Conditions

Entering ambient conditions allow Shooter's Reference to calculate wind drift corrections as well as air density compensation. U.S. Army Standard Metro conditions are the default.

## $\oplus$ wind speed

- Optional, in mph or kph
$\oplus$ wind direction
- Optional, in degrees, using meteorological convention (see illustration on page 13)
$\dagger$ elevation
- Optional, in feet or meters above sea level)
- If zero, temperature, humidity and pressure are used to calculate air density (most accurate method)
- If non-zero, then altitude is used to calculate air density (better than no air density correction)

SHOOTER'S REFERENCE V3

## setup solve ho

| cartridge an bullet caliber [in or mm ] | bullet parar bullet weight [gr] | bullet bc | $\begin{aligned} & \text { bullet } \\ & \text { model } \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| 0.338 | 250 | 0.587 |  |
| $\begin{gathered} \text { muzzle } \\ \text { velocity [fps] } \end{gathered}$ | muzzle energy [ft-lbs] | use bc | G5 |
| 2950 | 4830 |  |  |

ambient conditions

| wind speed <br> [mph] | wind direction <br> [deg] | elevation <br> [ft] |
| :---: | :---: | :---: |
| 15 | 270 | 0 |
| temperature <br> [deg F] | humidy <br> [rh \%] | pressure <br> [in Hg ] |
| 59.0 | 78 | 29.53 |
| firearm setup |  |  |
| fing <br> scope height <br> [in] | zero dist <br> [yds] | units <br> check for <br> metric |
| 1.5 | 200 |  |

firearm setup
scope height zero dist
[in] [yds]
1.5

200
units check for metricG6

## SEtUP [setup model parameters]

## Model Setup (continued)

## Ambient Conditions (continued)

- temperature
- Optional, in degrees Fahrenheit or Celsius
$\oplus$ humidity
- Optional, in RH percent
$\oplus$ pressure
- Optional, in inches of Mercury or hectoPascals

Tip: If exact ambient conditions are not available, a good guess at temperature and humidity while leaving the pressure at the default value will improve the ballistic model's results.

SHOOTER'S REFERENCE V3

## setup solve ho

| cartridge an bullet caliber [in or mm ] | bullet parar bullet weight [gr] | bullet bc | $\begin{aligned} & \text { bullet } \\ & \text { model } \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| 0.338 | 250 | 0.587 |  |
| muzzle velocity [fps] | muzzle energy [ft-lbs] | use bc | G5 |
| 2950 | 4830 |  |  |

ambient conditions

| wind speed [mph] | wind direction [deg] | elevation [ft] |
| :---: | :---: | :---: |
| 15 | 270 | 0 |
| temperature [deg F] | humidy <br> [rh \%] | pressure [in Hg ] |
| 59.0 | 78 | 29.53 |
| firear scope height [in] | setup zero dist [yds] | units <br> check for |
| 1.5 | 200 | metric |

firearm setup
scope height zero dist
[in] [yds]
1.5

200
units check for metricG6

## SEtUP [setup model parameters]

## Model Setup (continued)

## Firearm Setup

The model uses the scope mounting height and the zero distance to calculate the bore angle of the firearm relative to the line of sight. The centerline to centerline height of the scope relative to the barrel is critical to the accuracy of the model.
$\oplus$ scope height

- The centerline to centerline height of the scope or sights to the barrel
- Required, in inches or millimeters
- zero distance
- Required, in yards or meters


## Measurement Units

Metric units are used internally. Input and display units can be toggled at any time by checking/unchecking this box.
$\oplus$ input units

- Required, in yards or meters


## SHOOTER'S REFERENCE V3

## setup solve ho

| cartridge an bullet caliber [in or mm] | d bullet paran bullet weight [gr] | bullet bc | bullet mode |
| :---: | :---: | :---: | :---: |
| 0.338 | 250 | 0.587 |  |
| muzzle velocity [fps] | muzzle energy [ft-lbs] | use bc | G5 |
| 2950 | 4830 |  |  |

ambient conditions

| wind speed <br> [mph] | wind direction <br> [deg] |
| :---: | :---: |
| 15 | 270 |

firearm setup scope height zero dist

| [in] | [yds] | check for <br> metric |
| :---: | :---: | ---: |
| 1.5 | 200 |  |

## SOlVE [enter target data and solve model]

## Find a Solution

The target distance, bearing, and inclination angle are entered on the solve page. Press the solve button to calculate the solution.
$\oplus$ distance

- The line of sight distance to the target
- Required, in yards or meters
$\dagger$ bearing
- The target bearing
- Required, in degrees
© inclination angle
- The target inclination angle (see illustration on page 13)
- Required, in degrees

The line of sight distance (also referred to as the slant range) is the straight line distance as measured to the target. The ballistics model uses the Rifleman's Rule to calculate the horizontal distance to the target. This compensates for uphill or downhill shooting situations.

## SHOOTER'S REFERENCE V3

## solve hold tabl

target parameters
distance

[yds] | bearing |
| :---: |
| [deg] angle [deg] |

| 325 | 0 | 0 | solve |
| :---: | :---: | :---: | :---: |

solution

|  | solution <br> [inches] | correction |  |
| :--- | :---: | :---: | :---: |
| [moa] | [mils] |  |  |
| drop | -9.4 | U2.7 | U0.8 |
| drift | -9.0 | L2.6 | L0.8 |
| kinetic energy [ft-lb] |  | 3286 |  |
| velocity [fps] | 2433 |  |  |
| laser / los intercept [yds] | 30.3 |  |  |
| laser position on target [in] | 14.6 |  |  |



## SOlVE [enter target data and solve model]

The inclination angle is the angle of the target relative to the shooter. A $0^{\circ}$ inclination is horizontal, flat ground. Positive inclination angles indicate an uphill shot while negative inclination angles indicate a downhill shot. Please refer to Wikipedia for an explanation of the Rifleman's Rule.


Source: http://en.wikipedia.org/wiki/Rifleman's rule

## SHOOTER'S REFERENCE V3 <br> solve hold tabl

target parameters
distance bearing inclination [yds] [deg] angle [deg]

| 325 | 0 | 0 |
| :--- | :--- | :--- |

solution

|  | solution | correction |  |
| :---: | :---: | :---: | :---: |
|  | [inches] | [moa] | [mils] |
| drop | -9.4 | U2.7 | U0.8 |
| drift | -9.0 | L2.6 | L0.8 |


| kinetic energy [ft-lb] | 3286 |
| :--- | :--- |
| velocity [fps] | 2433 |

velocity [fps] 2433

| laser / los intercept [yds] | 30.3 |
| :--- | :--- |
| laser position on target [in] | 14.6 |



## SOlVE [enter target data and solve model]

The bearing is the compass bearing of the target.


Tip: Target bearing is the direction in which the firearm is pointing. Wind direction is where the wind is blowing from (meteorological convention).

## SHOOTER'S REFERENCE V3

## solve hold tabl

target parameters
distance bearing inclination
[yds] [deg] angle [deg]

| 325 | 0 | 0 | solve |
| :---: | :--- | :--- | :--- |

solution

|  | solution | correction |  |
| :--- | :---: | :---: | :---: |
|  | [inches] | [moa] | [mils] |
| drop | -9.4 | U2.7 | U0.8 |
| drift | -9.0 | L2.6 | L0.8 |

kinetic energy [ft-lb] 3286
velocity [fps] 2433

| laser / los intercept [yds] | 30.3 |
| :--- | :--- |
| laser position on target [in] | 14.6 |



## SOlVe [enter target data and solve model]

Click the solve button to calculate the solution.

Drop and drift are displayed in length units as well as mils and MOA's. "U" and "D" preceding a number refer to up and down while " L " and " $R$ " preceding a number refer to left and right sight adjustments.

For example, in the screenshot to the right, the sights should be adjusted up 2.7 MOA or 0.8 mils to account for bullet drop. 2.6 MOA or 0.4 mils left must be dialed-in to account for wind drift.

The kinetic energy and bullet velocity at the target distance are also displayed. Kinetic energy is displayed in either ft-lb or Joules. Velocity is displayed in feet per second (fps) or meters per second (mps).

## Bore Laser Sight

The laser bore sight solution displays the two key numbers required to sight-in a firearm at a desired zero distance when using a bore laser light such as the SITELITE $®^{8}$ Mag Laser Boresighters ${ }^{(B)}$.

The laser / LOS intercept is the distance at which the bore laser line and the line of sight cross. It is displayed in yards or meters. If you place a target at this distance, the laser dot on the target should be right in the center of the scope or on the front sight.

SHOOTER'S REFERENCE V3

## solve hold tabl

target parameters
distance bearing inclination [yds] [deg] angle [deg]

| 325 | 0 | 0 |
| :---: | :---: | :---: |

solution


## SOlVe [enter target data and solve model]

The laser position on target is the distance from the sight position to the laser dot on the target required to achieve the desired zero distance. The target distance is the value entered for distance under target parameters.


Tip: In addition to the target distance, the bore sight calculator requires the ballistics of the cartridge in use and the mounting height of the scope or sights. The cartridge ballistic specs can be manually entered in the setup page or by selecting a cartridge in the search page. Consult your laser bore sight manufacturer's user's manual for instructions specific to your model.

SHOOTER'S REFERENCE V3

## solve hold tab

target parameters
\(\left.$$
\begin{array}{c}\begin{array}{c}\text { distance } \\
\text { [yds] }\end{array} \\
\begin{array}{c}\text { bearing } \\
\text { [deg] }\end{array}\end{array}
$$ \begin{array}{c}inclination <br>

angle [deg]\end{array}\right]\)| 325 | 0 |
| :---: | :---: |

solution

|  | solution | correction |  |
| :---: | :---: | :---: | :---: |
|  | [inches] | [moa] | [mils] |
| drop | -9.4 | U2.7 | U0.8 |
| drift | -9.0 | L2.6 | L0.8 |

kinetic energy [ft-lb] 3286
velocity [fps] 2433
laser / los intercept [yds] 30.3
laser position on target [in] 14.6

## hold [sight picture]

## Mil-Dot Sight Picture

Once a solution is found, the hold page displays the "hold" position required to be on target at the distance, bearing, and inclination angle entered on the solve page. Holding the firearm such that the target is in the position indicated by the green dot, will place the shot on the target.

The vertical axis is labeled in half mil-dot increments with the ontarget distances corresponding to that vertical hold. The horizontal axis is also labeled in half mil-dot increments with the distances corresponding to wind drift.

For example, a 350 yard shot would require a vertical hold of just under 1 mil ( 352 yards) for drop and about 0.7 mils ( $0.7 \times$ 500 yards) for wind drift.

When metric units are selected, sight picture values are displayed in meters.

## SHOOTER'S REFERENCE V3

## hold table sigh



SHOOTER'S REF V3
Ballistics calculator for the shooting sports.

And it's FREE!

## table [view drop and drift correction table]

## Drop and Drift Table

Once a solution is found, the table page displays the drop and drift solution from 50 to 500 yards or meters at 5 yard or meter increments at a zero degree inclination angle.
"U" and "D" preceding a number refer to up and down while "L" and "R" preceding a number refer to left and right sight adjustments.

## SHOOTER'S REFERENCE V3

table sight-in r

| $\begin{gathered} \text { dist } \\ {[\mathrm{yds}]} \end{gathered}$ | drop [in] | drop <br> [mils] | drop <br> [moa] | drift <br> [in] | drift <br> [mils] | drift <br> [moa] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 185 | 0.6 | U0.1 | U0.3 | -2.9 | L0.4 | L1.5 |
| 190 | 0.4 | U0.1 | U0.2 | -3.0 | L0.4 | L1.5 |
| 195 | 0.2 | U0.0 | U0.1 | -3.2 | L0.5 | L1.6 |
| 200 | 0.0 | U0.0 | U0.0 | -3.4 | L0.5 | L1.6 |
| 205 | -0.2 | U0.0 | U0.1 | -3.5 | L0.5 | L1.6 |
| 210 | -0.4 | U0.1 | U0.2 | -3.7 | L0.5 | L1.7 |
| 215 | -0.6 | U0.1 | U0.3 | -3.9 | L0.5 | L1.7 |
| 220 | -0.9 | U0.1 | U0.4 | -4.1 | L0.5 | L1.8 |
| 225 | -1.1 | U0.1 | U0.5 | -4.3 | L0.5 | L1.8 |
| 230 | -1.4 | U0.2 | U0.6 | -4.4 | L0.5 | L1.8 |
| 235 | -1.7 | U0.2 | U0.7 | -4.6 | L0.5 | L1.9 |
| 240 | -2.0 | U0.2 | U0.8 | -4.8 | L0.6 | L1.9 |
| 245 | $-2.3$ | U0.3 | U0.9 | -5.0 | L0.6 | L2.0 |
| 250 | -2.6 | U0.3 | U1.0 | -5.3 | L0.6 | L2.0 |
| 255 | -3.0 | U0.3 | U1.1 | -5.5 | L0.6 | L2.0 |
| 260 | -3.3 | U0.4 | U1.2 | -5.7 | L0.6 | L2.1 |
| 265 | -3.7 | U0.4 | U1.3 | -5.9 | L0.6 | L2.1 |
| 60 | SIX SIGMA <br> Statistical tools for the six sigma practitioner. |  |  |  |  | And it's FREE! |

## sight-in [sight-in your rifle at the range]

## Sighting-in on the Range

The sight-in page provides a simple, non-model method of zeroing a firearm on the range.

## - target distance

- Required, in yards or meters
© vertical adjustment
- Required, in inches or centimeters
- The vertical distance to move the impact point. Enter a positive value to move the impact point up, a negative value to move the impact point down.


## $\oplus$ horizontal adjustment

- Required, in inches or centimeters
- The horizontal distance to move the impact point. Enter a positive value to move the impact point right, a negative value to move the impact point left.

Tip: Use 3-5 rounds and average the distance from the target center for best results.

## SHOOTER'S REFERENCE V3

## sight-in range

zero sight-in target distance and correction adjustment

| target distance [yds] | vertical adjustment [in] [up (+) down ( - )] | horizontal adjustment [in] [right (+) left ( - )] |
| :---: | :---: | :---: |
| 100 | 3.6 | -3.6 |
| solution |  |  |
| scope adjustment | vertical moa mils U3.4 U1.0 | horizontal moa mils $\qquad$ |

To calculate scope adjustment, enter distance to target and distance of group center from target center. Use $3-5$ rounds and average distance for best results.

And it's
FREE!

## range [estimate target range using mil scope]

## Estimating Range Using a Mil/MOA Scope

The range page provides a simple method of estimating the range of a target given its actual size and apparent size in mils or MOA.
$\dagger$ actual size

- Required, in inches or centimeters
- The actual height of the target area being measured
- scope size
- Required, in mils or MOA
- The apparent height of the target area being measured
$\oplus$ scope units
- Required, choose mils or MOA
- Determines table increment display
© table increment
- Required, choose $1 / 8^{\text {th }}$ or $1 / 10^{\text {th }}$ increments
- Determines range table increment display

SHOOTER'S REFERENCE V3

## range convert

target range estimator

| actual size [in] | solve |
| :---: | :---: |
| 72 |  |
|  | solution |
| scope size [mils] | est. distance [yds] |
| 4 | 500 |
| scope units | size [mils] dist [yds] |
| $\checkmark$ mils | $3.7 \quad 541$ |
|  | 3.8526 |
| moa | 3.9513 |
| table increment | $4.0 \quad 500$ |
| 1/8th | $4.1 \quad 488$ |
|  | $4.2 \quad 476$ |
| 1/10th | 4.3 465 |

BE SURE OF YOUR TARGET

## convert [convert distances to mils and moa]

## Converting Mils or MOA

The convert page provides a simple calculator to determine the value of Mils or MOA's at a given distance.
$\oplus$ distance

- Required, in yards or meters
- The target distance

The value of both a Mil and MOA (or quarter fractions) is displayed in inches or centimeters.

## SHOOTER'S REFERENCE V3 <br> convert safety

mil/moa converter
distance
[yds]
100
solution

|  | unit fraction |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| value of: | 1 | $3 / 4$ | $1 / 2$ | $1 / 4$ |
| mil [in] | 3.6 | 2.7 | 1.8 | 0.9 |
| moa [in] | 1.0 | 0.8 | 0.5 | 0.3 |

i
Enter distance to calculate value of a moa or mil. Unit fraction is fraction of moa or mil.

## safety rules [read them. learn them. live them.]

Lt. Col. Jeff Cooper (USMC), founder of Gunsite Academy, author, columnist, professor, WW II and Korean War combat veteran, and innovator of the Modern Technique of the Pistol had four simple safety rules:

- ALL FIREARMS ARE ALWAYS LOADED
- NEVER LET THE MUZZLE OF A FIREARM POINT ANYTHING YOU ARE NOT WILLING TO DESTROY
- KEEP YOUR FINGER OFF THE TRIGGER UNTIL YOUR SIGHTS ARE ON THE TARGET
- BE SURE OF YOUR TARGET

THE IMPORTANCE OF THESE RULES CAN NOT BE STRESSED ENOUGH. THE MOST IMPORTANT SAFETY FEATURE WHEN HANDLING A FIREARM IS THE ONE BETWEEN YOUR EARS, NOT THE ONES ON THE FIREARM.

## SHOOTER'S REFERENCE V3

## safety rules he

All firearms are always loaded.

Never let the muzzle of a firearm point at anything you are not willing to destroy.
Keep your finger off the trincer unless vour

## APPENDIX

- Model internals
$\oplus$ Model performance


## model internals [how it works]

Shooter's Reference's ballistics model is based on Newtonian physics. This section describes the inner workings of the model in mathematical terms. Basic knowledge of physics and calculus is required to understand the model but is not a prerequisite for using the application. Several good books available as well as Wikipedia's articles on external ballistics and related topics as well as many other Internet sources. Our preferred source is Bryan Litz's excellent book.

Litz, Bryan (2011), Applied Ballistics for Long Range Shooting (2 $2^{\text {nd }}$ edition), Cedar Springs, MI, Applied Ballistics LLC.

The ballistics model can be divided into three functional blocks.

- Ambient Conditions
- Firearm Setup
- Projectile Motion Simulation


## Ambient Conditions

There are three factors that are important to calculating an accurate trajectory: air density, the speed of sound, and crosswind speed.

Air density can be calculated one of two ways by the model. The preferred method is to use temperature, pressure and humidity at the shooter's location. Alternatively, the model can use elevation and sea level temperature, pressure and humidity or their approximation. In reality, for hunting distances out to 500 yards, air density is a very small factor in bullet drop or drift, typically on the order of tenths of an inch. By comparison, we see several inches of variation when comparing trajectories generated by utilizing the G7 model instead of the G1+BC model (see comparisons in Appendix).

## model internals [how it works]

To determine air density from temperature, pressure and humidity we employ the following equations:

First, we calculate the saturation pressure for water vapor from a rather complicated magical formula that uses temperature only.

$$
p_{\text {sat }}=e^{\left(\frac{\frac{77.435+0.0057-\frac{7235}{T}}{T}}{T^{8.2}}\right)}
$$

Next, we calculate the partial pressure of the water vapor from the relative humidity and the saturation pressure. This is a very small number, on the order of $1-2 \%$ of the total atmospheric pressure.

$$
p_{w v}=\left(\frac{R H}{100}\right) \times p_{s a t}
$$

Before we calculate the partial pressure of dry air, we need to know the local atmospheric pressure. This can be measured directly or obtained from your favorite weather website.

If the local atmospheric pressure can not be determined, an approximation can be made based on altitude and either actual nearby or standard sea level pressure.

$$
p=p_{0} e^{-\left(\frac{h}{h_{0}}\right)}
$$

The partial pressure of dry air can be determined by simple subtraction:

$$
p_{d r y}=p-p_{w v}
$$

The density of a mixture of dry air and water follows:

$$
\rho_{\text {humid }}=\frac{p_{d r y} \times M_{d r y}+p_{w v} \times M_{w v}}{R \times T}
$$

The speed of sound varies with air density and is given by:

$$
c=\sqrt{\gamma \times \frac{p}{\rho_{\text {humid }}}}
$$

## model internals [how it works]

Firearm Setup

Bore angle is the barrel cant that results from the difference between the line of sight to the target (what you see through the scope or sights) and the launch angle required to be on target at the zero distance on flat ground. Shooter's Reference allows the user to choose an arbitrary zero distance.


Angle Exaggerated For Illustration Purposes
Source: http://en.wikipedia.org/wiki/Rifleman's rule
Most manufacturers' ballistics tables assume a height of 1.5 inches but chances are that your sights or scope are not mounted at that height. This is a significant source of error. The centerline to centerline height of the sights or scope above the barrel is required to calculate the bore angle. This measurement is critical and should be taken with care.

A zero distance that is close to the target range is recommended. For example, when targets are likely to be around 75 yards away, set the zero distance to 75 yards.

Bore angles are typically very small, around 0.05 to 0.10 degrees. However, a small variation can result in several inches of error at 500 yards. Shooter's Reference calculated zero at the actual zero distance is $\pm 0.05$ inches ( $\pm 1.27 \mathrm{~mm}$ ).


Angles Exaggerated for Illustration
Source: http://en.wikipedia.org/wiki/Rifleman's rule
The zero distance and scope height entered on the setup page is used to generate a custom drop table for your cartridge and firearm. The ballistics model uses an iterative process that takes into account the cartridge, bullet and ambient conditions to determine the bore angle.

## model internals [how it works]

The zero correction in mils and moa is displayed on the solve page and the bore angle is used by the ballistics model along with the inclination angle to generate the solution at the target distance as well as the custom drop table.

## Projectile Motion Simulation

Once the ambient conditions, firearm, and cartridge/bullet parameters are set, the ballistics model generates a solution at the user specified distance on the solve page and for each distance point in the accompanying drop/drift table page.

Bullet drag is calculated using one of two formulas depending on whether the user has selected the "use BC" option on the setup page. It is recommended that the "use BC" option is not used and that instead a bullet model that most closely matches the bullet in use be chosen. BC's are not constant with speed although manufacturers quote a single $B C$, typically based on the G1 model in their cartridge specifications.

Using the manufacturer's BC introduces a systemic error and results in larger errors. The Appendix shows model results for three common cartridges with and without BC compensation. For modern low drag bullets, the G7 model without $B C$ compensation provides the best results.

The ballistics model implements a table of drag coefficients for each of the supported bullet models developed by the Army Ballistics Research Lab. These are discussed in the bullet models section. A new drag is calculated for each trajectory point based on the bullet's velocity at that point.

The two equations for calculating drag are:

$$
\begin{aligned}
& F_{\text {drag }}=\frac{\rho \times v^{2} \times C_{\text {drag }} \times A}{2} \\
& C_{\text {drag }}=\frac{C_{G 1 C D} \times m}{B C \times D^{2}} \quad[\text { If } \mathrm{BC} \text { is used }]
\end{aligned}
$$

## model internals [how it works]

The ballistics model simulates the path of the projectile, or bullet, by repeatedly calculating its drag, velocity, acceleration, and position at intervals of either 0.5 yards or meters depending on whether Imperial or metric units are selected.

The initial conditions are determined by the muzzle velocity and the launch angle. The launch angle is determined by the inclination angle to the target and the bore angle of the "zeroed" firearm.

The model performs calculations based on units of time, $t$, required to travel the model distance interval.

$$
d t=\frac{d x}{v_{x(0)}}
$$

The initial velocity is the muzzle velocity.

$$
v_{(0)}=v_{m u z z l e}
$$

Since the projectile is launched at an angle (at a minimum the bore angle on flat ground), it is necessary to determine its velocity in both the $x$ and y axes. In addition, the forces of gravity and drag act differently in both axes so those must also be treated separately.

The initial velocities in the $x$ and $y$ axes are given by:

$$
\begin{aligned}
& v_{x(0)}=v_{(0)} \times \cos (\theta+\delta) \\
& v_{y(0)}=v_{(0)} \times \sin (\theta+\delta)
\end{aligned}
$$

Acceleration is given by the general vector formula:

$$
\vec{a}=\frac{\vec{F}}{m}
$$

Acceleration (deceleration in this case) can be approximated as follows for each axis:

$$
a_{x}=-\frac{F_{d r a g}}{m} \quad \text { and } \quad a_{y}=-G+\frac{F_{d r a g}}{m}
$$

## model internals [how it works]

Given velocity, acceleration and time, a new position can be calculated.

$$
\begin{aligned}
& x_{(t+1)}=x_{(t)}+v_{x(t)} \times d t+\frac{a_{x}}{2} \times d t^{2} \\
& y_{(t+1)}=y_{(t)}+v_{y(t)} \times d t+\frac{a_{y}}{2} \times d t^{2}
\end{aligned}
$$

New velocities are similarly updated.

$$
\begin{gathered}
v_{x(t+1)}=v_{x(t)}+a_{x} \times d t \\
v_{y(t+1)}=v_{y(t)}+a_{y} \times d t \\
v_{(t+1)}=\sqrt{v_{x(t+1)}{ }^{2}+v_{y(t+1)}{ }^{2}}
\end{gathered}
$$

Since the projectile is now moving more slowly, the time to travel to the next computation point also needs to be recalculated..

$$
d t=\frac{d x}{v_{x(t+1)}}
$$

The process repeats until the drop and drift table is completed and the target distance reached.

## Wind Drift

Wind drift is calculate using the Army Ballistics Lab method described in: Leupold, Herbert A. (October 1996), Wind Drift of Projectiles: A Ballistics Tutorial, ARL-TR-1124.

The full text may be downloaded from:

## http://www.dtic.mil/dtic/tr/fulltext/u2/a317305.pdf

The amount of drift requires the calculation of the perpendicular wind speed, the actual time of flight, and the time of flight in a vacuum. The time of flight in a vacuum is simply the time to travel the horizontal distance at the muzzle velocity since there is no drag to slow the projectile's velocity while in flight.

$$
t_{v}=\frac{x_{h}}{v_{0}}
$$

The wind drift is calculated with the following equation:

$$
x_{d}=v_{w} \times\left(t_{a}-t_{v}\right)
$$

## model internals [howitworks]

## Kinetic Energy

Kinetic energy is calculated at the target range. While kinetic energy is a good indicator of a bullet's ability to stop and/or kill game, it is not the only factor. The user of this program should consult the manufacturer's recommendations for specific game. A small bullet with high kinetic energy does not perform the same as a large bullet with the same kinetic energy.

Kinetic energy is calculated as follows:

$$
E_{k}=\frac{m \times v^{2}}{2}
$$

## model internals [how it works]

| VARIABLE | DESCRIPTION |
| :---: | :--- |
| $T$ | temperature |
| $R H$ | relative humidity |
| $p$ | barometric pressure |
| $p_{0}$ | sea level barometric pressure |
| $p_{s a t}$ | vapor saturation pressure |
| $p_{w V}$ | partial pressure of water vapor |
| $p_{d r y}$ | partial pressure of dry air |
| $\rho_{h u m i d}$ | density of humid air |
| $v_{w}$ | perpendicular (cross) wind speed |
| $h$ | elevation |
| $h_{0}$ | height of the atmosphere |
| $c$ | speed of sound |
| $R$ | universal gas constant |
| $M_{w v}$ | molar mass of water vapor |
| $M_{d r y}$ | molar mass of dry air |
| $\gamma$ | adiabatic index |


| VARIABLE | DESCRIPTION |
| :---: | :--- |
| $d x$ | calculation interval distance |
| $d t$ | calculation interval time |
| $\vec{F}$ | force vector |
| $m$ | mass |
| $\vec{a}$ | acceleration vector |
| $D$ | diameter of bullet |
| $F_{d r a g}$ | drag force |
| $C_{d r a g}$ | drag coefficient |
| $C_{G 1 C D}$ | drag coefficient of G 1 std. model |
| $a_{x}, a_{y}$ | acceleration at time t in x or y |
| $v_{(t)}$ | velocity at time t |
| $v_{x(t)}, v_{y(t)}$ | velocity at time t in x or y |
| $x_{(t)}, y_{(t)}$ | position at time t |
| $x_{h}$ | horizontal distance |
| $t_{v}$ | time of flight in a vacuum |
| $t_{a}$ | actual time of flight |

## model internals [how it works]

Standard Bullet Models

Shooter's Reference allows the user to select various standard models that are used to calculate bullet drag. By choosing the model that best fits your bullet, you can improved the accuracy of the results. Shooter's Reference continuously adjusts drag based on the instantaneous velocity of the bullet based on the selected bullet shape model.

The descriptions of the bullet models in the table to the right refer to the terms "blunt ogive" "secant ogive" with and "tangent ogive." These describe the shape of the bullet's nose and date back to nose cone designs for rockets.

More information on nose cone designs is available on Wikipedia:
http://en.wikipedia.org/wiki/Nose cone design

| MODEL | DESCRIPTION |
| :---: | :--- |
| G1 | Ingalls. Flatbase. 2 caliber blunt ogive <br> nose. Generally used by manufactures <br> to express BC. |
| $\mathbf{G 2}$ | Aberdeen J projectile. |
| $\mathbf{G 5}$ | Short 7.5 <br> tangent ogive nose. |
| $\mathbf{G 6}$ | Flatbase. 6 caliber secant ogive nose. |
| G7 <br> Default | Long $7.5^{\circ}$ boat-tail. 10 caliber tangent <br> ogive nose. Best model for low drag <br> bullets. Some manufacturers provide <br> G7 BC's in addition to G1 BC's. |
| $\mathbf{G 8}$ | Flatbase. 10 caliber secant ogive <br> nose. |
| $\mathbf{G L}$ | Blunt lead nose. <br> Source: http://en.wikipedia.org/wiki/External ballistics |

## model internals [how it works]

Manufacturers typically provide a BC (ballistics coefficient) that is based on the G1 model. Some have also started providing G7 based BC's. However, best results are achieved without using BC compensation because BC's vary with velocity.

The G1 and GL models will yield very similar results, typically within 0.5 inches ( 1.3 cm ) of drop at 500 yards ( 457 m ). The G2, G5, G6, G7, and G8 models also yield similar results. Since most long range shooters are using very low drag boat-tails for best performance, the G7 model yields the best results.

Results of comparisons of manufacturer's data compared with the model solutions, with and without BC compensation are provided for the Winchester 308, Winchester 338 Lapua Magnum and the Winchester 300 Magnum.


G1


G7


G1
GL


G7


Bullet Shape and Recommended Model


## model performance data ${ }_{[300}$ winchester magnum]

| Distance (yds) |  | 0 | 100 | 200 | 300 | 400 | 500 | $\Delta$ @ 500 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V (fps) | Manufacturer | 2900 | 2726 | 2558 | 2396 | 2240 | 2090 |  |
|  | SR Model G7 | 2900 | 2730 | 2566 | 2406 | 2249 | 2093 | 3 |
|  | SR Model G1 + BC | 2900 | 2710 | 2526 | 2348 | 2178 | 2018 | -72 |
| E (ft-lbs) | Manufacturer | 3548 | 3134 | 2760 | 2422 | 2117 | 1843 |  |
|  | SR Model G7 | 3548 | 3145 | 2777 | 2441 | 2133 | 1847 | 4 |
|  | SR Model G1 + BC | 3548 | 3097 | 2691 | 2325 | 2001 | 1718 | -125 |
| D (in) | Manufacturer | -1.5 | 1.6 | 0.0 | -6.9 | -19.9 | -39.8 |  |
|  | SR Model G7 | -1.5 | 1.6 | 0.0 | -7.1 | -20.8 | -42.7 | -2.9 |
|  | SR Model G1 + BC | -1.5 | 1.6 | 0.0 | -7.3 | -21.8 | -44.9 | -5.1 |
| W (in) | Manufacturer | 0.0 | 0.6 | 2.4 | 5.5 | 10.1 | 16.4 |  |
|  | SR Model G7 | 0.0 | 0.7 | 2.4 | 5.4 | 9.9 | 16.0 | -0.4 |
|  | SR Model G1 + BC | 0.0 | 0.7 | 2.7 | 6.2 | 11.3 | 18.2 | 1.8 |



## model performance data ${ }_{[338}$ winchester lapua magnum]

| Distance (yds) |  | 0 | 100 | 200 | 300 | 400 | 500 | $\Delta$ @ 500 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V (fps) | Manufacturer | 2950 | 2789 | 2634 | 2484 | 2339 | 2199 |  |
|  | SR Model G7 | 2950 | 2785 | 2625 | 2469 | 2316 | 2166 | -33 |
|  | SR Model G1 + BC | 2950 | 2775 | 2606 | 2441 | 2282 | 2130 | -69 |
| E (ft-lbs) | Manufacturer | 4830 | 4318 | 3851 | 3426 | 3037 | 2685 |  |
|  | SR Model G7 | 4830 | 4305 | 3824 | 3382 | 2977 | 2603 | -82 |
|  | SR Model G1 + BC | 4830 | 4275 | 3768 | 3307 | 2890 | 2519 | -166 |
| D (in) | Manufacturer | -1.5 | 1.5 | 0.0 | -6.5 | -18.5 | -37.1 |  |
|  | SR Model G7 | -1.5 | 1.5 | 0.0 | -6.7 | -19.8 | -40.4 | -3.3 |
|  | SR Model G1 + BC | -1.5 | 1.5 | 0.0 | -6.8 | -20.2 | -41.4 | -4.3 |
| W (in) | Manufacturer | 0.0 | 0.5 | 2.1 | 4.9 | 8.8 | 14.3 |  |
|  | SR Model G7 | 0.0 | 0.6 | 2.2 | 5.1 | 9.2 | 14.9 | 0.6 |
|  | SR Model G1 + BC | 0.0 | 0.6 | 2.4 | 5.4 | 9.9 | 15.9 | 1.6 |



## model performance data ${ }_{[308 \text { winchester] }}$

| Distance (yds) |  | 0 | 100 | 200 | 300 | 400 | 500 | $\Delta @ 500$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V (fps) | Manufacturer | 2820 | 2597 | 2385 | 2183 | 1990 | 1808 |  |
|  | SR Model G7 | 2820 | 2598 | 2384 | 2175 | 1967 | 1767 | -41 |
|  | SR Model G1 + BC | 2820 | 2575 | 2342 | 2122 | 1921 | 1749 | -59 |
| E (ft-lbs) | Manufacturer | 2648 | 2246 | 1894 | 1586 | 1319 | 1089 |  |
|  | SR Model G7 | 2648 | 2248 | 1892 | 1576 | 1289 | 1040 | -49 |
|  | SR Model G1 + BC | 2648 | 2209 | 1826 | 1499 | 1229 | 1018 | -71 |
| D (in) | Manufacturer | -1.5 | 1.8 | 0.0 | -8.0 | -23.3 | -47.2 |  |
|  | SR Model G7 | -1.5 | 1.8 | 0.0 | -8.3 | -25.2 | -53.3 | -6.1 |
|  | SR Model G1 + BC | -1.5 | 1.8 | 0.0 | -8.7 | -26.4 | -55.8 | -8.6 |
| W (in) | Manufacturer | 0.0 | 0.8 | 3.3 | 7.8 | 14.4 | 23.3 |  |
|  | SR Model G7 | 0.0 | 0.9 | 3.4 | 7.8 | 14.5 | 24.0 | 0.7 |
|  | SR Model G1 + BC | 0.0 | 0.9 | 3.7 | 8.6 | 16.1 | 26.2 | 2.9 |



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